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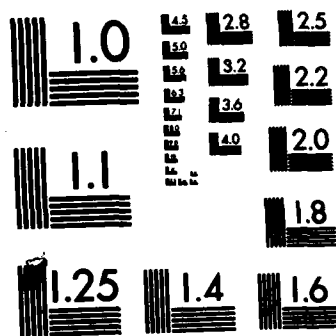
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An Experimental Estimate of the Electron-Tunneling  
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by

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AN EXPERIMENTAL ESTIMATE OF THE ELECTRON-TUNNELING  
DISTANCE FOR SOME OUTER-SPHERE ELECTROCHEMICAL REACTIONS

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Abstract

Estimates of the reaction zone thickness over which electron tunneling can effectively occur for the outer-sphere electrochemical reduction of some Cr(III) complexes are obtained by comparing the observed work-corrected rate constants with unimolecular rate constants for the electroreduction of structurally similar surface-bound Cr(III) reactants. Effective reaction zone thicknesses of ca 0.1 - 0.3 Å and ca 5 Å are obtained for outer-sphere electron transfer with Cr(III) reactants containing predominantly aquo or ammine ligands, respectively. This indicates that the former reactions are marginally nonadiabatic whereas the latter are decidedly adiabatic at their respective planes of closest approach. These findings are compatible with the greater reactant-electrode separation distances previously noted for Cr(III) aquo relative to ammine complexes resulting from the more extensive hydration sheath surrounding the former reactants. Comparisons with recent calculations performed for some outer-sphere homogeneous reactions suggest that efficient electron tunneling takes place over roughly comparable distances at metal-electrolyte interfaces and in bulk solution.

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An important question in the treatment of electron-transfer reactions concerns the magnitude of the frequency factor,  $A$ , in the expression

$$k_{ob} = A \exp(-w_p/RT) \exp(-\Delta G_{et}^*/RT) \quad (1)$$

where  $k_{ob}$  is the observed rate constant,  $w_p$  is the work required to bring the reactants together (or the reactant to the electrode surface), and  $\Delta G_{et}^*$  is the free-energy barrier for the elementary electron-transfer step.

Although sophisticated theoretical methods have been developed for evaluating  $\Delta G_{et}^*$  from structural and thermodynamic information, there remains considerable uncertainty as to the numerical values of the frequency factor for outer-sphere pathways.<sup>1,2</sup>

In the recent literature it has been emphasized that outer- as well as inner-sphere redox reactions in homogeneous solution and at electrode surfaces can usually be viewed as involving formation of a reactive precursor complex from initially separated reactants followed by the rate-determining transfer step.<sup>1-5</sup> Thus the observed rate constant can be formulated as

$$k_{ob} = K_p k_{et} \quad (2)$$

where  $K_p$  is the equilibrium constant for forming the precursor state and  $k_{et}$  is the rate constant describing the elementary electron-transfer step. When applied to outer-sphere pathways, this approach can be termed an "encounter preequilibrium" treatment. It views the reaction as taking place via the unimolecular activation of a weakly interacting reactant pair having a suitably close proximity and geometrical configuration to enable electron transfer to occur once the appropriate nonequilibrium nuclear configuration has been achieved.<sup>1b,c,2b,5c</sup>

According to the encounter-preequilibrium treatment, the frequency factor can be expressed as<sup>1b,c,5c</sup>

$$A = \Gamma_n \nu_n \kappa_{el}^0 K_0 \quad (3)$$

where  $\Gamma_n$  is the nuclear tunneling factor,  $\nu_n$  is the effective frequency for activating nuclear reorganization modes,  $\kappa_{el}^0$  is the electronic transmission coefficient at the distance of closest approach of the reactants and  $K_0$  is the statistical part of the precursor stability constant  $K_p$  where

$$K_p = K_0 \exp(-w_p/RT) \quad (4)$$

For electrochemical reactions the statistical factor  $K_0^e$  can be expressed simply as<sup>5c</sup>

$$K_0^e = \delta r_e \quad (5)$$

where  $\delta r_e$  is the thickness of a "reaction zone" beyond the plane of closest approach within which the reactant must reside in order to contribute significantly to the overall reaction rate. The value of  $\delta r_e$  is determined by the need for the reactant and surface to be in sufficiently close proximity to achieve significant overlap of donor and acceptor orbitals, and hence nonzero values of the transmission coefficient  $\kappa_{el}$  for a given reactant orientation (vide infra). The composite term  $\kappa_{el}^0 K_0^e (\equiv \kappa_{el}^0 \delta r_e)$  appearing in Eq (3) for electrochemical reactions can therefore be considered to be an "effective reaction zone thickness". If  $\kappa_{el}^0 < 1$ , the reaction is termed "nonadiabatic", whereas "adiabatic" processes are those for which  $\kappa_{el}^0 \sim 1$ . Since the magnitude of  $\delta r_e$  is determined by the dependence of  $\kappa_{el}$  upon the donor-acceptor separation distance, markedly



smaller values of  $\kappa_{e1}^0 \delta r_e$  are anticipated for the former compared to the latter processes as a result of smaller values of  $\delta r_e$  as well as  $\kappa_{e1}^0$ .

The statistical factor for homogeneous reactions,  $K_0^h$ , is more complex than  $K_0^e$  yet entirely analogous, corresponding to the probability of finding one reactant within a reaction zone of thickness  $\delta r_h$  beyond the bimolecular contact distance. This term can be estimated approximately from<sup>1c,e,2b,c</sup>

$$K_0^h = 4\pi N \bar{r}^2 \delta r_h / 10^3 \quad (6)$$

where  $N$  is the Avogadro number, and  $\bar{r}$  is the distance between the reacting centers when in contact.

Recent ab initio calculations for some homogeneous outer-sphere reactions<sup>2</sup> indicate that  $\kappa_{e1}$  can be substantially below unity even at a relatively small internuclear separation  $r$ , decreasing sharply with increasing  $r$ . This corresponds to relatively small values of  $\kappa_{e1}^0 \delta r_h$  ( $< 1 \text{ \AA}$ , vide infra).<sup>1c,e</sup> It would be extremely desirable to obtain an experimental measure of such quantities. In the approach described here, estimates of  $\kappa_{e1}^0 \delta r_e$  for several outer-sphere electrochemical processes are obtained by a relatively direct method involving the comparison of rate constants for these pathways with those for structurally related electrochemical reactions occurring via geometrically well-defined ligand-bridged transition states. The results provide evidence that heterogeneous, as well as homogeneous, electron-transfer processes can be significantly nonadiabatic.

#### Data Analysis

The virtue of comparing rate parameters for corresponding electrochemical reactions occurring via outer- and inner-sphere (ligand-bridged) pathways can be seen by noting that in contrast to the former, unimolecular rate constants for the electron-transfer step involving a ligand-bridged precursor state,

$k_{et}^{is}$  ( $\text{sec}^{-1}$ ), can often be determined directly from the overall rate constant,  $k_{ob}^{is}$ , using Eq (2) since  $K_p$  can be found from<sup>5a,c</sup>

$$K_p = \Gamma_p / C_b \quad (7)$$

where  $\Gamma_p$  is the measured reactant surface concentration ( $\text{mole cm}^{-2}$ ) corresponding to a given bulk reactant concentration  $C_b$ . The values of  $k_{et}^{is}$  can be expressed as

$$k_{et}^{is} = \Gamma_n \nu_n \kappa_{el}^{is} \exp(-\Delta G_{et}^* / RT) \quad (8)$$

where  $\kappa_{el}^{is}$  is the electronic transmission coefficient for the ligand-bridged reaction pathway. In view of Eqs (1) and (3)-(5), the work-corrected rate constant for the corresponding outer-sphere electrochemical pathway,  $k_{corr}^{os}$ , can be expressed as

$$k_{corr}^{os} = \Gamma_n \nu_n \kappa_{el}^{os} \cdot \delta r_e \cdot \exp(-\Delta G_{et}^* / RT) \quad (9)$$

Provided that  $\Delta G_{et}^*$ ,  $\Gamma_{el}$ , and  $\nu_n$  are unaffected by surface attachment at a given electrode potential (vide infra), evaluation of the rate ratios  $k_{corr}^{os} / k_{et}^{is}$  enable estimates of  $\kappa_{el}^o \delta r_e$ , at least relative to  $\kappa_{el}^{is}$ , to be obtained. This procedure will now be utilized to estimate the effective electron-tunneling distances for some outer-sphere Cr(III) reductions at the mercury-aqueous interface.

Pertinent kinetic and thermodynamic data are assembled in Table I for the electroreduction of three  $\text{Cr}^{III}(\text{NH}_3)_5\text{X}$  complexes, where  $\text{X} = \text{NCS}^-$ ,  $\text{N}_3^-$ , and  $\text{Cl}^-$ , and five  $\text{Cr}^{III}(\text{OH}_2)_5\text{X}$  complexes, where  $\text{X} = \text{OH}_2$ ,  $\text{SO}_4^{2-}$ ,  $\text{F}^-$ ,  $\text{NCS}^-$ , and  $\text{N}_3^-$ . The data were extracted from refs 5a, 6, and 7. These reactions were chosen because rate constants corresponding to both inner- and outer-sphere pathways,  $k_{et}^{is}$  and  $k_{corr}^{os}$  respectively, can be obtained directly

or estimated from experimental data.<sup>5c</sup> Several of these reactions have been examined previously in a related discussion of the relative energetics of inner- and outer-sphere pathways.<sup>5a</sup>

The work-corrected rate constants,  $k_{\text{corr}}^{\text{os}}$ , were determined from the corresponding observed rate constants,  $k_{\text{ob}}^{\text{os}}$ , using the electrostatic double-layer corrections as outlined in ref. 6 (see footnotes to Table I). Of the three Cr(III) ammine reactants,  $\text{Cr}(\text{NH}_3)_5\text{N}_3^{2+}$  and  $\text{Cr}(\text{NH}_3)_5\text{Cl}^{2+}$  exhibit mixed electroreduction kinetics which enable both  $k_{\text{ob}}^{\text{os}}$  and  $k_{\text{ob}}^{\text{is}}$  to be obtained.<sup>5a,6</sup> The latter values are combined with estimates of  $K_p$  obtained under the same conditions from kinetic probe measurements<sup>5a,8</sup> to yield values of  $k_{\text{et}}^{\text{is}}$  by using Eq (2). The common electrode potential of -600 mV vs. the saturated calomel electrode (sce) was chosen so to minimize the extent of data extrapolation that is involved. The estimate of  $k_{\text{et}}^{\text{is}}$  for  $\text{Cr}(\text{NH}_3)_5\text{N}_3^{2+}$  reduction ( $1 \text{ sec}^{-1}$ ) is close to that observed for  $\text{Cr}(\text{NH}_3)_5\text{NCS}^{2+}$  reduction ( $0.5 \text{ sec}^{-1}$ ); this supports the validity of the former estimate in view of the closely similar coordination properties of  $-\text{N}_3^-$  and  $-\text{NCS}^-$ .<sup>5a</sup>

Each of the five Cr(III) aquo reactants in Table I undergoes electroreduction via sufficiently rate-dominating outer- or inner-sphere pathways so that only  $k_{\text{ob}}^{\text{os}}$  or  $k_{\text{et}}^{\text{is}}$  can be evaluated for each reactant. Nevertheless, an approximate estimate of  $k_{\text{corr}}^{\text{os}}/k_{\text{et}}^{\text{is}}$  for these structurally related reactions can still be obtained as follows. As we have noted previously,<sup>7</sup> the values of  $k_{\text{corr}}^{\text{os}}$  for  $\text{Cr}(\text{OH}_2)_6^{3+}$ ,  $\text{Cr}(\text{OH}_2)_5\text{SO}_4^+$ , and  $\text{Cr}(\text{OH}_2)_5\text{F}^{2+}$  reduction are closely similar when evaluated at their respective formal potentials. This indicates that the intrinsic electron-transfer barrier is approximately independent of the nature of the sixth ligand, even though the coordinating properties of  $\text{OH}_2$ ,  $\text{SO}_4^{2-}$  and  $\text{F}^-$  differ widely. These values of  $k_{\text{corr}}^{\text{os}}$ , listed in Table I, are therefore also likely to be close to those for  $\text{Cr}(\text{OH}_2)_5\text{NCS}^{2+/+}$  and  $\text{Cr}(\text{OH}_2)_5\text{N}_3^{2+/+}$ .

which cannot be measured but for which the corresponding values of  $k_{et}^{is}$  are known, enabling the desired estimate of  $k_{corr}^{os}/k_{et}^{is}$  to be obtained (Table I).

### Discussion

Inspection of Table I shows that the resulting values of  $k_{corr}^{os}/k_{et}^{is}$  for Cr(III) aquo reduction, ca.  $0.2 \text{ \AA}$ , are ca. 10-30 fold smaller than those for the Cr(III) ammine reductions, ca  $5 \text{ \AA}$ . Quantitative interpretation of these results can be made by referring to Eqs (8) and (9). Of the various terms,  $\nu_n$  and  $\Gamma_n$  will almost certainly have the same values for the corresponding inner- and outer-sphere pathways. Thus  $\nu_n$  is determined chiefly by the metal-ligand stretching frequencies<sup>5c</sup> and  $\Gamma_n$  is usually close to unity, being dependent upon the magnitude of  $\Delta G_{et}^*$  rather than the transition-state geometry.<sup>1b</sup> The reorganization energy  $\Delta G_{et}^*$  may differ significantly for corresponding inner- and outer-sphere pathways, arising both from differences in the inner-shell (metal-ligand) and outer-shell (solvent) reorganization terms. Ligand bridging may yield some decreases in the inner-shell component of  $\Delta G_{et}^*$  arising from the influence of surface attachment on the Cr(III)-ligand bonding. However, we have found scant evidence for such catalyses with Cr(III)/(II) and Co(III)/(II) electrode reactions, even at surfaces such as platinum and gold that bind inorganic ligand bridges much more strongly than does mercury.<sup>9</sup>

Surface attachment may yield an alteration in the outer-shell component of  $\Delta G_{et}^*$  since this is predicted to diminish as the distance between the redox center and the surface decreases, as a result of greater image stabilization of the transition state.<sup>11</sup> With the azido and isothiocyanato bridges, the redox center is estimated to lie about  $5\text{-}6 \text{ \AA}$  from the surface.<sup>10</sup> Provided that the outer-sphere transition state is formed with the reactant in contact with a monolayer of inner-layer water molecules (vide infra), the redox center will

be about 6.5 Å from the surface, based on a reactant crystallographic radius of 3.5 Å and a water molecule diameter of 3 Å.<sup>6</sup> On the basis of the well-known relation for the outer-shell component of  $\Delta G_{et}^*$  due to Marcus,<sup>11,12</sup>  $k_{corr}^{os}$  is predicted to increase by only ca. 50% upon decreasing the reactant-electrode separation from 7 to 6 Å, and by only ca 3-fold from 7 to 5 Å. It therefore appears likely that  $\Delta G_{et}^*$  only differs to a small extent between corresponding outer- and inner-sphere pathways involving thiocyanate and azide bridges. The similar values of  $k_{corr}^{os}/k_{et}^{is}$  seen for  $Cr(NH_3)_5Cl^{2+}$  and  $Cr(NH_3)_5N_3^{2+}$  reduction (Table I), even though the Cr(III) - surface distance is expected to be ca. 2 Å smaller for the former reaction, lends support to this assertion.

To a first approximation, then, from Eqs (8) and (9) the rate ratios  $k_{corr}^{os}/k_{et}^{is}$  for the present system can be related to the effective reaction zone thickness for the outer-sphere pathways,  $\kappa_{el}^0 \delta r_e$ , simply by

$$k_{corr}^{os}/k_{et}^{is} \approx \kappa_{el}^0 \delta r_e / \kappa_{el}^{is} \quad (10)$$

Since the ligand bridge should facilitate overlap between the surface donor and Cr(III) acceptor orbitals it is anticipated that the inner-sphere pathways are adiabatic, i.e.  $\kappa_{el}^{is} \sim 1$ . If indeed  $\kappa_{el}^{is} \sim 1$ , then the values of  $k_{corr}^{os}/k_{et}^{is}$ , ca 5 and 0.2, can be identified directly with the effective reaction zone thickness  $\kappa_{el}^0 \delta r_e$  for the ammine and aquo reactants, respectively. Even if  $\kappa_{el}^{is} < 1$ , it is likely to have essentially the same value for both pentaammine- and pentaquo Cr(III) reductions bridged by azide and isothiocyanato ligands since the Cr(III)-surface distance and hence the degree of orbital overlap should be determined by the bridging ligand. It therefore appears certain that  $\kappa_{el}^0 \delta r_e$  is markedly larger for the ammine compared to the aquo reactants.

A persuasive explanation for this striking result is to be found in the differences in the location of the outer-sphere reaction sites that have been noted previously for these reactions.<sup>6,12,13</sup> Thus the reduction rates of  $\text{Cr}(\text{OH}_2)_6^{3+}$  and other Cr(III) aquo complexes are markedly less sensitive to variations in the double-layer potential profile than are the reduction rates of  $\text{Cr}(\text{NH}_3)_6^{3+}$  and related Cr(III) amines.<sup>6</sup> These results provide evidence that the Cr(III) aquo reaction sites are constrained to lie significantly further from the electrode surface. This is consistent with the larger hydrated radii for aquo versus ammine reactants due to the more extensive ligand-solvent hydrogen bonding exhibited by the former complexes.<sup>6,14</sup> From an analysis of the observed double-layer effects, we have estimated that the reaction site for  $\text{Cr}(\text{OH}_2)_6^{3+}$  reduction lies 6-7 Å from the surface, whereas that for  $\text{Cr}(\text{NH}_3)_6^{3+}$  reduction is about 1.5 Å closer.<sup>6</sup> (Although the absolute reactant-electrode distances are subject to as much as 1 - 1.5 Å uncertainty, the relative distances for the aquo versus ammine reactants are rather more reliable). It is therefore to be expected that  $\kappa_{e1}^0$  will be larger for the ammine than for the aquo reactants unless the reactant-surface electronic coupling is sufficient to provide adiabatic pathways ( $\kappa_{e1}^0 \approx 1$ ) in both cases.

In order to interpret the individual values of  $\kappa_{e1}^0 \delta r_e$ , it is advantageous to consider the encounter preequilibrium treatment in a little more detail. Since  $\kappa_{e1}$  will depend upon the donor-acceptor separation distance within the reaction zone of thickness  $\delta r_e$ , strictly speaking one should express the overall observed rate constant in terms of an integral of "local" values of  $k_{et}$ , each being associated with a particular spatial position and orientation of the reactant and hence individual values of  $\kappa_{e1}$ ,  $w_p$ , and  $\Delta G_{et}^*$ .<sup>2b</sup> The dependence of  $\kappa_{e1}$  upon the separation distance,  $r$ , for nonadiabatic pathways

can be approximated by<sup>2a,c</sup>

$$\kappa_{e1}(r) = \kappa_{e1}^0 \exp[-\alpha(r-\sigma)] \quad (11)$$

where  $\sigma$  is the separation distance corresponding to closest approach,

and  $\alpha$  is a constant which is typically estimated to lie in the range ca.

$1 - 2 \text{ \AA}^{-1}$ .<sup>2c,15</sup> Consequently, if  $\kappa_{e1}^0 < 1$  (i.e. the reaction is nonadiabatic at the plane of closest approach), the effective value of  $\delta r_e$  will be equal  $\alpha^{-1}$ . On the other hand, if  $\sigma$  is sufficiently small so that  $\kappa_{e1} \approx 1$  not only at the distance of closest approach but also for a significant distance,  $\chi$ , beyond it, we expect that roughly

$$\delta r_e = \chi + \alpha^{-1} \quad (12)$$

Equation (12) therefore provides a general relationship where  $\chi = 0$

if  $\kappa_{e1}^0 < 1$ , and  $\chi > 0$  if  $\kappa_{e1}^0 \approx 1$ .

Figure 1 is a schematic representation of the dependence of  $\kappa_{e1}$  upon  $r$ . The magnitude of  $\kappa_{e1}^0 \delta r_e$  will equal the area under the curve bounded by the distance of closest approach, for example the shaded area A'A"C. Taking  $\alpha \approx 1.5 \text{ \AA}^{-1}$ , it follows that  $\kappa_{e1}^0 \delta r_e < 0.5 \text{ \AA}$  if  $\kappa_{e1}^0 < 1$ , whereas  $\kappa_{e1}^0 \delta r_e > 0.5 \text{ \AA}$  if  $\kappa_{e1}^0 \approx 1$ . The above estimate of  $\kappa_{e1}^0 \delta r_e$  for the Cr(III) aquo reactions, ca  $0.1 - 0.3 \text{ \AA}$ , therefore suggests that  $\kappa_{e1}^0 < 1$  at the plane of closest approach for the aquo cations, so that  $\chi \approx 0$ . However, this estimate of  $\kappa_{e1}^0 \delta r_e$  may be ca 1.5 to 2-fold too small as a result of the likely differences in  $\Delta G_{et}^*$  between the inner- and outer-sphere pathways noted above, although it may be too large if  $\kappa_{e1}^{is} < 1$ . Another factor which would decrease the apparent value of  $\kappa_{e1}^0 \delta r_e$  is the possibility that a

specific reactant orientation is required either to enable the reactant to approach the electrode more closely or to provide more effective coupling of the surface donor and Cr(III) acceptor orbitals. Such factors have recently been considered in detail for  $\text{Fe}(\text{OH}_2)_6^{3+/2+}$  self exchange.<sup>2</sup> In any case, we conclude that outer-sphere electron transfer involving the Cr(III) aquo reactants only approaches adiabaticity for electron-tunneling distances very close to the plane of closest approach of these cations (represented by B'B" in Fig. 1), around 6-7 Å from the electrode surface.

On the other hand, the estimate of  $\kappa_{el}^0 \delta r_e$  for the Cr(III) amines, ca 5 Å, suggests that electron transfer to these reactants remains adiabatic even for reaction sites several Angstroms from the plane of closest approach (represented by A'A" in Fig. 1). The exact value of  $\kappa_{el}^0 \delta r_e$  for the ammine reactants is in one respect subject to greater uncertainty than for the aquo reactants in that the magnitude of the work-term ("double-layer") correction upon  $k_{ob}$  is somewhat greater for the former.<sup>6</sup> Moreover, the work-term correction employed assumes that the reaction occurs only at the outer Helmholtz plane (oHp), whereas the large value of  $\kappa_{el}^0 \delta r_e$  suggests that the effective reaction zone is relatively thick. Given that the ammine reactants can probably penetrate inside the oHp, this work-term correction may well be an underestimate, so that  $k_{corr}^{os}$  and hence  $\kappa_{el}^0 \delta r_e$  are actually smaller than the present values. Given that the aquo reactants are marginally adiabatic at their plane of closest approach, from the reaction site differences noted above it would be expected that  $\chi \sim 2$  Å for the amines, yielding  $\kappa_{el}^0 \delta r_e \sim 2-3$  Å. One factor which may enhance  $\kappa_{el}^0 \delta r_e$  for the ammine versus the aquo complexes is the likely greater ligand character of the acceptor orbital on the former reactants,<sup>2c</sup> leading to greater electrode-reactant orbital overlap at a given electrode-reactant separation distance. The difference in the effective reaction zone thickness between the aquo



and ammine reactants is therefore roughly compatible with the likely differences in the reaction sites if the dependence of  $\kappa_{e1}$  upon the surface-reactant separation is similar for these reactants, with  $\kappa_{e1}$  decreasing below unity for surface-reactant separations greater than ca. 6 Å.

Taking  $\Gamma_n = 2.5$  and  $\nu_n = 1.2 \times 10^{13} \text{ sec}^{-1}$  for the present reactions,<sup>16</sup> it is deduced from Eqs (3) and (5) that the overall frequency factor A is ca.  $6 \times 10^4$  and  $1.5 \times 10^6 \text{ cm sec}^{-1}$  for the aquo and ammine reactants, respectively. Both these values are somewhat larger than the frequency factor, ca.  $5 \times 10^3 \text{ cm sec}^{-1}$ , derived from the conventional collisional model assuming adiabatic behavior.<sup>5c,17</sup> It should be noted that the encounter preequilibrium treatment employed here represents a departure from the collisional model since the latter views the reaction as being consummated only by collisions between the reactant and the electrode surface (or a coreactant).<sup>5c</sup>

It is of interest to compare the above estimate of A for the Cr(III) aquo reactants with that obtained for  $\text{Cr}(\text{OH}_2)_6^{3+}$  reduction under the same conditions from the temperature dependence of  $k_{\text{corr}}^{\text{OS}}$ . We can write<sup>17</sup>

$$k_{\text{corr}}^{\text{OS}} = A \exp(\Delta S_i^*/R) \exp(-\Delta H_i^*/RT) \quad (13)$$

where  $\Delta S_i^*$  and  $\Delta H_i^*$  are the work-corrected "ideal" entropies and enthalpies of activation which form the components of  $\Delta G_{\text{et}}^*$  at the particular electrode potential at which  $k_{\text{corr}}^{\text{OS}}$  is obtained.<sup>17,18</sup> The activation enthalpy  $\Delta H_i^*$  can be obtained directly from the Arrhenius slope of  $\ln k_{\text{corr}}^{\text{OS}}$  versus  $(1/T)$ , being measured at a constant electrode potential using a nonisothermal cell arrangement.<sup>17</sup> The value of  $\Delta S_i^*$  can be obtained from<sup>17,19</sup>

$$\Delta S_i^* = \alpha_{\text{corr}} \Delta S_{\text{rc}}^\circ + \Delta S_{\text{int}}^* \quad (14)$$

where  $\alpha_{\text{corr}}$  is the work-corrected transfer coefficient,  $\Delta S_{\text{rc}}^\circ$  is the so-called

reaction entropy of the redox couple concerned,<sup>14a</sup> and  $\Delta S_{\text{int}}^*$  is the intrinsic activation entropy.<sup>20</sup> From the data given in ref 17, at -800 mV vs. sce,  $k_{\text{corr}}^{\text{os}} = 5.5 \times 10^{-5} \text{ cm sec}^{-1}$  (25°C),  $\Delta H_{\text{f}}^* = 17.5 \text{ kcal. mol}^{-1}$ ,<sup>21</sup>  $\alpha_{\text{corr}} = 0.50$ ,  $\Delta S_{\text{rc}}^{\circ} = 49 \text{ cal. deg}^{-1} \text{ mol}^{-1}$ , and  $\Delta S_{\text{int}}^* = -3.5 \text{ cal. deg}^{-1} \text{ mol}^{-1}$ .<sup>20</sup> Inserting these data into Eqs (13) and (14) yields  $A = 9 \times 10^3 \text{ cm sec}^{-1}$ . (This calculation cannot be performed for Cr(III) ammine reductions since the  $\Delta S_{\text{rc}}^{\circ}$  values are not known with sufficient accuracy.)

The ca 7-fold discrepancy between this and the above estimate of  $A$  probably arises in part from the very approximate nature of Eq (14). This relation presumes that the transition-state entropy is unaffected by the proximity of the reacting ions to the electrode surface, whereas it is likely that  $\Delta S_{\text{f}}^*$  and  $\Delta H_{\text{f}}^*$  are much more sensitive than is the overall barrier  $\Delta G_{\text{et}}^*$  to the solvating environment at the interface and the bulk solution. Indeed, we have found that the activation parameters for these and other reactions are rather more sensitive than is  $k_{\text{corr}}^{\text{os}}$  to the nature of the electrode material, surprisingly small frequency factors being typically obtained at solid metal surfaces.<sup>22</sup>

### Conclusions

The foregoing treatment provides a relatively direct, albeit approximate, experimental method for evaluating the effective electron-tunneling distances for outer-sphere electrochemical reactions. It exploits both the close relationship between the energetics of corresponding inner- and outer-sphere electrode reactions and the information that can be derived<sup>6,13</sup> on the reactant-electrode separation distance from the magnitude of the double-layer effects in electrochemical kinetics. A strictly analogous approach cannot be employed for homogeneous processes due to the inevitable changes in reactant coordination between otherwise related inner-

and outer-sphere pathways and the lack of a means for subtly altering the electrostatic interactions between ionic reactants in solution.

Although it would not be surprising if similar differences in the internuclear distances and hence  $\kappa_{el}^0 \delta r$  also arise between aquo and ammine complexes in homogeneous electron-transfer reactions, the solvating environments may be sufficiently different to that pertaining to the present electrochemical reactions<sup>23</sup> to bring other factors to the fore. Indeed, the larger rate ratios for Co(III) ammine versus aquo reactants observed at mercury electrodes relative to that obtained with a given reductant in homogeneous solution<sup>12</sup> suggest that these differences in  $\kappa_{el}^0 \delta r$  may well be smaller in the latter environment. Nevertheless, the present finding that outer-sphere electrochemical reactions can be at least marginally nonadiabatic bears a close resemblance to the interpretation of some anion catalytic effects upon homogeneous outer-sphere reactions between cationic complexes<sup>25</sup> as well as to the results of the recent ab initio calculations noted above.<sup>2</sup> Similar calculations have yet to be performed for electron-transfer processes at metal surfaces; they would provide an invaluable guide to the further interpretation of the experimental data.

The present results therefore are at variance with a previous suggestion that the effective electron-tunneling probabilities should be much larger at metal surfaces due to the multitude of electronic energy states in the vicinity of the Fermi level that are available for coupling with the reactant orbitals.<sup>26</sup> Further support to the present findings is given by our observation that both the unimolecular rate constants and frequency factors for the electroreduction of pentaamminecobalt(III) bound to a mercury surface via organic bridges are decreased markedly upon interruption of bond

conjugation in the bridging ligand.<sup>9,27</sup> These observations serve to highlight the previously neglected role of nonadiabatic electron tunneling in influencing electron-transfer reactivity at electrode surfaces as well as in homogeneous solution.

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- (21) The effective value of  $\Delta H^\ddagger$  is slightly ( $0.3 \text{ kcal. mol}^{-1}$ ) larger than the values given in ref. 17 since these were determined by assuming that the frequency factor is slightly temperature dependent as expected from the collision model utilized in ref. 17.
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TABLE I. Kinetic and Thermodynamic Data for the One-Electron Reduction of Cr(III) Complexes at the Mercury-Aqueous Interface at 25°C.

Reactant	Pathway <sup>a</sup>	-E mv. vs sce	<sup>b</sup> $k_{ob}$ cm sec <sup>-1</sup>	<sup>c</sup> $k_{corr}^{os}$ cm sec <sup>-1</sup>	<sup>d</sup> $K_p$ cm	<sup>e</sup> $k_{et}^{is}$ sec <sup>-1</sup>	$k_{corr}^{os}/k_{et}^{is}$ Å
Cr(NH <sub>3</sub> ) <sub>5</sub> NCS <sup>2+</sup>	is	600	1 x 10 <sup>-5</sup>		2 x 10 <sup>-5</sup>	0.5	5-10
Cr(NH <sub>3</sub> ) <sub>5</sub> N <sub>3</sub> <sup>2+</sup>	os	600	6 x 10 <sup>-7</sup>	1 x 10 <sup>-7</sup>			
	is	600	~5 x 10 <sup>-7</sup>		5 x 10 <sup>-7</sup>	~1	
Cr(NH <sub>3</sub> ) <sub>5</sub> Cl <sup>2+</sup>	os	600	3 x 10 <sup>-6</sup>	6 x 10 <sup>-7</sup>			~5
	is	600	1 x 10 <sup>-5</sup>		~1 x 10 <sup>-6</sup>	~10	
Cr(OH <sub>2</sub> ) <sub>6</sub> <sup>3+</sup>	os	655	7.5x10 <sup>-6</sup>	2.5x10 <sup>-6</sup>			~0.1-0.3
Cr(OH <sub>2</sub> ) <sub>5</sub> SO <sub>4</sub> <sup>+</sup>	os	705	4.6x10 <sup>-6</sup>	3.5x10 <sup>-6</sup>			
Cr(OH <sub>2</sub> ) <sub>5</sub> F <sup>2+</sup>	os	860	6 x 10 <sup>-6</sup>	2 x 10 <sup>-6</sup>			
Cr(OH <sub>2</sub> ) <sub>5</sub> NCS <sup>2+</sup>	is	720	4 x 10 <sup>-3</sup>		~4 x 10 <sup>-6</sup>	1 x 10 <sup>3</sup>	
Cr(OH <sub>2</sub> ) <sub>5</sub> N <sub>3</sub> <sup>2+</sup>	is	~720	1.2x10 <sup>-4</sup>		~2 x 10 <sup>-7</sup>	2 x 10 <sup>3</sup>	

<sup>a</sup>is = inner-sphere (ligand-bridged) pathway; os = outer-sphere pathway

<sup>b</sup>Observed rate constant for overall electrode reaction following is or os pathway indicated at electrode potential, E, listed in adjacent column. Values of  $k_{ob}$  for Cr(III) aquo complexes determined at formal potential for Cr(III)/(II) couple. Data taken from refs. 5a, 6 and 7.

<sup>c</sup>Work-corrected rate constant for outer-sphere pathway. Determined from corresponding value of  $k_{ob}$  using  $k_{corr}^{os} = k_{ob} \exp[(Z-0.5)\phi_{rp}]$ , where Z is the reactant charge number, and  $\phi_{rp}$  is the average potential at the reaction plane (see refs 6 and 7 for details).

<sup>d</sup>Stability constant for the inner-sphere precursor state, determined from Eq (7); taken from ref. 5a.

<sup>e</sup>Unimolecular rate constant for electron-transfer step involving ligand-bridged intermediate. Obtained from listed values of  $k_{ob}$  and  $K_p$  using Eq. (2).

Figure Caption

Schematic plot of electronic transmission coefficient  $\kappa_{e1}$  for an outer-sphere electrochemical reaction against the reactant-electrode separation distance  $r$ . A'A" and B'B" represent anticipated planes of closest approach for Cr(III) ammine and aquo, reactants, respectively. The shaded and cross-hatched areas represent the corresponding values of the "effective reaction zone thickness"  $\kappa_{e1}^0 \delta r_e$  for these reactants.



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